Opinion dynamics



November 6, 2018

An overview

- Human societies and interactions are extremely complex, with so many aspects/parameters that makes it "hopeless" to apprehend it
- However, they are characterized by global regularities and transitions from disorder to order (they seem to have regularities)
 - Language formation
 - "Culture" formation
 - Emergence of consensus
- Opinion dynamics (at least partly) seem to be apprehensible
- Opinions are important, because
 - They shape our everyday life (social, political, private)
 - They drive our behavior
 - Acting "adequately" on a certain situation: it is a matter of opinions / beliefs

- Aim: to model (understand and predict) the formation of opinions within various populations, under various conditions
- Relevant general questions include:
 - What are the fundamental interaction mechanisms that allow for the emergence of
 - consensus on an issue
 - a shared culture
 - a common language
 - collective motion
 - a hierarchy?
 - What favors the homogenization process? What hinders it?
- "Unfortunately": Opinion formation is a complex process affected by the interplay of different elements, including the
 - Individual predisposition / family background
 - Surrounding people (topology of the social network)
 - external information (e.g. public media)
 - Background knowledge
 - Etc, etc.

Typically...

models consider a

- finite number of connected agents
- each possessing opinions as variables,
- opinions change according to certain rules (which are also subjects of assumptions)
- resulting from interactions, either with peers or other sources.

Opinions:

- Variables:
 - one dimensional/multidimensional vector
 - discrete (the components can assume a finite number of states)
 - or continuous (values in the domain of real numbers)

Connections:

- Topology of the interaction NW (what is realistic?)
- "Heritage" from physics: lattices or all-to-all (MF); hardly realistic in social context
- "Rules" to model how people form opinions;
 "agent-based models"

Drawbacks of the models:

- many simplifications;
- many of the omitted parameters (most probably) have a fundamental effect in the final dynamics

Success in:

- Agreement
- Cluster formation
- Transition between order (consensus) and disorder (fragmentation)

Binary opinions

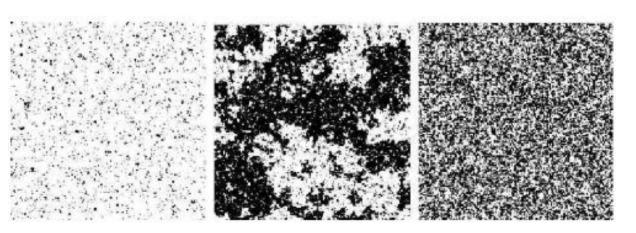
- Discrete, one dimensional
- 0/1; yes/no; etc



Interpretation in op. dyn: political questions
 infection models: infected / not
 market behavior: selling/buying

The first attempts – the Ising model metaphor

- Consider a collection of N spins (agents): s_i
- They can assume two values: +/- 1
- Each spin is energetically pushed to be aligned with its nearest neighbors.
- The total energy is: $H = -\frac{1}{2} \sum_{\langle i,j \rangle} s_i s_j$ (the sum runs on the pairs of nearest-neighbors)
- Elementary move:
- a single spin flip is accepted with probability $\exp(-\Delta E/k_BT)$ $-\Delta E$: change in the energy
 - T: temperature (In ferromagnetic systems thermal noise injects fluctuations tends to destroy order)
 - Critical temperature T_c : above: the system is macroscopically disordered under: long-range order is established



Snapshots of equilibrium configurations of the Ising model (from left to right) below, at and above T_c .

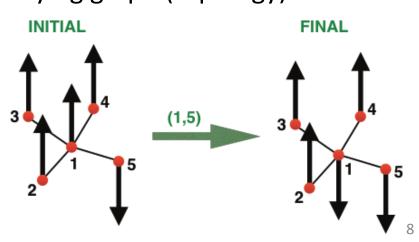
Relation to opinion dynamics models

- Each agent has one opinion represented as a spin: a choice between two options
- Spin couplings: peer interactions
- Magnetic field: external information / propaganda
- Too simple, but attractive because of the phase transition
- Early 1980's
- Potts model (1951)
- a generalization of the Ising model
- Each spin can assume one out of q values
- equal nearest neighbor values are energetically favored.
- The Ising model corresponds to the special case q=2
- (Very first op. dyn model by physicist: 1971, Weidlich)

Voter model

- Originally introduced to analyze competition of species, early 1970s
- Rather crude description of any real process
- Popular: it is one of the very few non-equilibrium stochastic processes that can be solved exactly in any dimension
- its name stems from its application to electoral competitions
- The model:
 - each agent in a population of N holds one of two discrete opinions: s
 = +/- 1
 - agents are connected by an underlying graph (topology)
 - At each time step:
 - a random agent i is selected (1) along with one of its neighbors j (5) and the agent takes the opinion of the neighbor: s_i=s_i

(alignment *not* to the majority, but to a random neighbor)

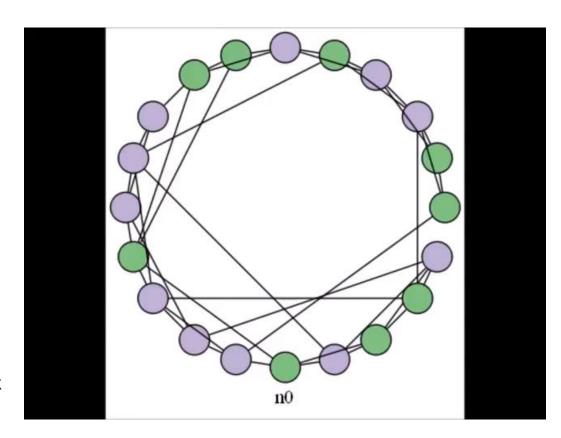


Behavior of the Voter model

- Has been extensively studied
- People are modeled as vertices in a d-dimensional hyper-cubic lattice.
- For finite system: for any dimension *d* of the lattice, the voter dynamics always leads to one of the two possible consensus states:
 - each agent with the same opinion s = 1 or s = -1.
- The probability of reaching one or the other state depends on the initial state of the population.
- Time needed for reaching the consensus state:
 - $d = 1: T_N \sim N^2$
 - d = 2: $T_N \sim N \ln N$
 - $d > 2: T_N \sim N$
- For infinite systems: consensus is reached only if d ≤ 2

Extensions of the voter model

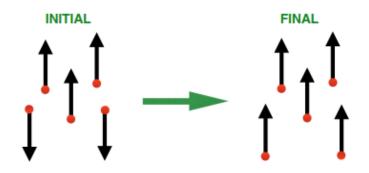
- Introduction of "zealots": individuals who do not change their opinion ("quenched disorder")
- Constrained voter model:
 - agents can be leftist, rightist, centralist;
 - Extremists do not talk to each other (discrete analogue of the bounded confidence model)
- Communication is based on various NW



Voter model on a small world network https://www.youtube.com/watch?v=VmhSTdrsimk

Majority rule model

- Motivation: describing public debates
- (Galam, 2002)
- Definition:
 - Population of N agents
 - A fraction p_{\perp} of agents has opinion +1
 - $p_{\perp} = 1 p_{\perp}$ has opinion -1
 - Everybody can communicate with everybody else
 - At each interaction:
 - A group of r agents are selected at random ("discussion group")
 - Consequence of this interaction: each agents take the majority opinion inside the group
 - r is taken from a given distribution at each step
 - If r is odd: there is always a clear majority
 - If r is even: in case of tie: a bias is introduced in favor of one of the options (Inspired by the principle of "Social inertia" holing that people are reluctant to accept a reform if there is no clear majority in its favor)



Basic features of the MR model

- Original definition:
 - There is a *threshold fraction* p_c such that if $p_0^+ > p_c$, then all agents will have opinion +1 in the long run
 - Time needed for the consensus: $T_N \sim \log N$
 - If the group sizes r are odd: $p_c(r) = 1/2$ (due to the symmetry)
 - If they can be even too: $p_c < 1/2$, that is, the favored opinion will eventually win, even if it was originally in minority
- For fixed odd r group size & mean field approach: analytically solvable for both finite N and for $N \rightarrow \infty$

Many variants and modifications

An extension: Public debates with incomplete scientific data

- Motivation: to model public debates driven by incomplete scientific data
 - nobody can claim absolute certainty
 - evolution theory, global warming and H1N1 pandemic influenza
- Two types of agents:
 - Floaters (can be convinced)
 - Inflexible agents (do not change their opinions)
- Result:
 - inflexible agents decide the result of the debate
 - a fair discourse in a public debate will most likely lead to losing
 - exaggerated claims are very useful for winning.
- A strategy for winning a debate: the acquisition of as many inflexible agents as possible

(Serge Galam: Public debates driven by incomplete scientific data: The cases of evolution theory, global warming and H1N1 pandemic influenza, Physica A, 2010, Vol 389, Pages 3619-3631)

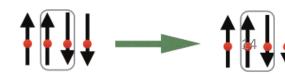
Sznajd model

- Main observation: a group of individuals with the same opinion can influence their neighbors more than one single individual. ("Social validation")
- One dimensional lattice
- Binary opinion
- A pair of neighboring agents i and i+1 determines the opinions of their two nearest neighbors i-1 and i+2
- If the agents of the pair share the same opinion, they successfully impose their opinion on their neighbors. If they disagree, each agent imposes its opinion on the other agent's neighbor
- Opinions are updated in a random sequential order

if
$$s_i = s_{i+1}$$
, then $s_{i-1} = s_i = s_{i+1} = s_{i+2}$



if $s_i \neq s_{i+1}$, then $s_{i-1} = s_{i+1}$ and $s_{i+2} = s_i$



Behavior of the Sznajd model

- Starting from a totally random initial configuration (both opinions are equally distributed), two types of stationary states appear:
 - consensus, with all spins up (m = 1) or all spins down (m = -1), with probability $\frac{1}{4} + \frac{1}{4} = \frac{1}{2}$
 - a stalemate, with the same number of up and down spins in antiferromagnetic order (m = 0). This is a consequence of the $s_i \neq s_{i+1}$ case, that favors antiferromagnetic configurations, and has a probability 1/2 to be reached.

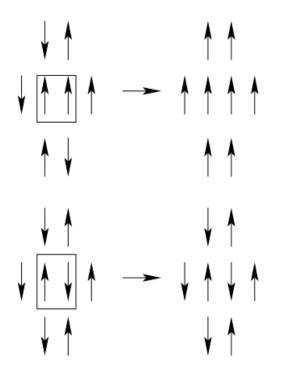
(Due to the up-down symmetry of the model.)

Critique (observation)

- Since the very introduction, it has been argued that:
 - a distinctive feature is that here the information flows from the initial pair of agents towards their neighbors (in contrast with other opinion dynamics models in which agents are influenced by their neighbors).
 - Because of that the Sznajd model was supposed to describe how opinions spread in a society
- Behera and Schweitzer (2003) shows that:
 - in 1D the direction of the information flow is irrelevant
 - \rightarrow dynamics is equivalent to a *voter* dynamics.
 - Difference compared to the classic voter model:
 - agents are not influenced by their nearest neighbors but by their next-tonearest neighbors
 - In Sznajd: a *pair* of agents is updated at a time, whereas in the voter model only one spin. This introduces a factor of two in the average relaxation time.
 - → Does not respect the principle of social validation which originally motivated its introduction, as each spin is influenced only by a single spin, not by a pair

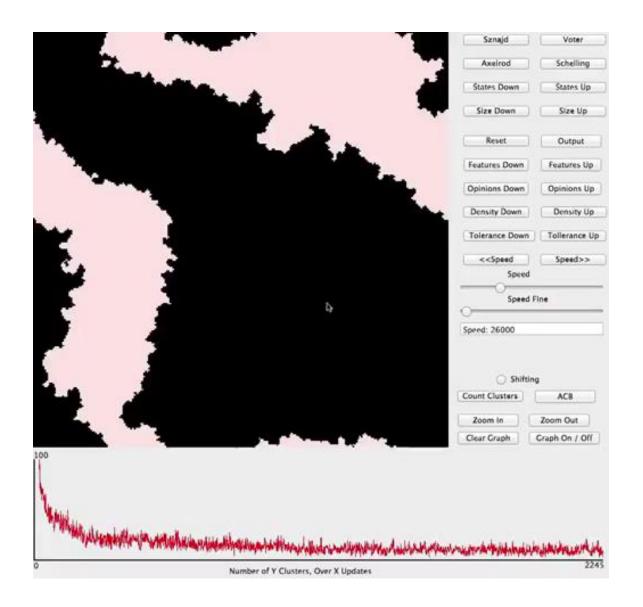
Update of the Sznajd model

- Rule $s_i \neq s_{i+1}$ is unrealistic, and was soon replaced/removed
- Most popular alternative: only the ferromagnetic rule (agreement) holds, so the neighbors of a disagreeing agents' pair maintain their opinions.
- Extensions of the Sznajd model usually adopt this prescription



On the square lattice, a pair of neighboring agents affect the opinions of their six neighbors, but only if they agree.

A pair of neighboring agents with the same opinion convince all their neighbors (top), while they have no influence if they disagree (bottom).



Cayne Byron:
"My Sznajd
Model
implementation.
Video just
running Q=2
number of
states in a
256x256 lattice.
Implemented in
OpenGL. "

Social impact theory

- Bibb Latané (psychologist), 1981:
- social impact: any influence on individual feelings, thoughts or behavior that is created from the real, implied or imagined presence or actions of others.
- The impact of a social group on a subject depends on:
 - The number of individuals within the group
 - Their convicting power
 - Their distance from the subject (spatial proximity or closeness in an abstract space of personal relationships)
- Original model, a cellular automata was introduced by Latané (1981) and refined by Nowak et al (1990).

Social impact theory – the model

- A population of N individuals
- Each individual i is characterized by
 - an opinion $\sigma_i = \pm 1$
 - Persuasiveness p_i : the capability to convince someone to change opinion (a real value)
 - Supportiveness: s_i: the capability to convince someone to keep its opinion (a real value)
 (these are assumed to be random)
- The distance between agents i and j d_{ij}
- α >2 parameter defining the how fast the impact decreases with the distance

$$I_i = \left[\sum_{j=1}^N \frac{p_j}{d_{ij}^{\alpha}} (1 - \sigma_i \sigma_j)\right] - \left[\sum_{j=1}^N \frac{s_j}{d_{ij}^{\alpha}} (1 + \sigma_i \sigma_j)\right]$$

Persuasive impact (to change)

supportive impact (to keep opinion)

$$\sigma_i(t+1) = -sgn[\sigma_i(t)I_i(t) + h_i]$$

h_i: random field representing all other sources (e.g. mass media)

a spin flips if the pressure in favor of the opinion change overcomes the pressure to keep the current opinion ($I_i > 0$ for vanishing h_i)

General behavior of the social impact model

- In the absence of individual fields:
 - the dynamics leads to the dominance of one opinion over the other, but not to complete consensus.
 - If the initial magnetization is about zero:
 - large majority of spins in the same opinion with stable domains of spins in the minority opinion state.
- In the presence of individual fields:
 - these minority domains become metastable: they remain stationary for a very long time, then they suddenly shrink to smaller clusters, which again persist for a very long time, before shrinking again, and so on ("staircase dynamics").
- Many modification / extensions:
 - Learning
 - Presence of a strong leader
 - Etc.

Missing aspects:

- Memory: reflecting past experience
- A finite velocity for the exchange of information between agents
- A physical space, where agents move.
 (Schweitzer and Holyst, 2000), including the above parameters
- Education
- Belief system, etc.

Continuous opinions

- In many cases more realistic
- Requires different framework
 - Concepts like "majority" or "opinion equality" don't work
 - Has a different 'history'
- First studies (end of 1970's and 80's):
 - Aimed to study the conditions under which a panel of experts would reach a common decision ("consensus")
 - By applied mathematicians
- Typically:
 - Initial state: population of N agents with randomly assigned opinions, represented by real value within some interval.
 discrete op. dyn. ↔ all agents start with different opinions
 - Possible scenarios: more complex with opinion clusters emerging in the final stationary state:
 - one cluster: consensus,
 - two clusters: polarization
 - more clusters: fragmentation

Bounded confidence (BC) models

- In principle: each agent can interact with every other
- In practice: (often) there is a real discussion only if the opinions are sufficiently close:

bounded confidence

- In the literature: introducing a real number ε: "uncertainty" or "tolerance", such that:
- An agent with opinion x, only interacts with those whose opinion lies in the interval $]x-\epsilon$, $x+\epsilon[$

Deffuant model

- population of N agents
- nodes of a graph: agents may discuss with each other if they are connected.
- Initially: each agent i is given an opinion x_i randomly chosen from the interval [0, 1].
- Dynamics:
 - random binary encounters, i.e., at each time step, a randomly selected agent discusses with one of its neighbors, also chosen at random.
 - Let i and j be the pair of interacting agents at time t, with opinions $x_i(t)$ and $x_i(t)$
 - if the difference of the opinions $x_i(t)$ and $x_j(t)$ exceeds the threshold ε , nothing happens
 - If $|x_i(t) x_i(t)| < \varepsilon$, then

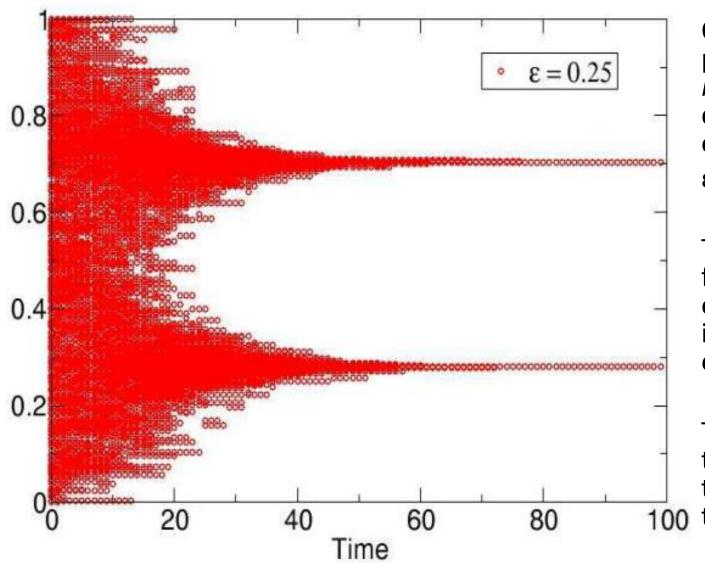
•
$$\mu$$
: convergence param.
 (μ in [0, 1/2]) $x_j(t)$

$$x_i(t+1) = x_i(t) + \mu[x_j(t) - x_i(t)]$$
$$x_j(t+1) = x_j(t) + \mu[x_i(t) - x_j(t)]$$

Behavior of the Deffuant model

- For any value of ϵ and μ , the average opinion of the agents' pair is the same before and after the interaction \rightarrow the global average opinion (1/2) of the population is invariant
- Patches appear with increasing density of agents
- Once each cluster is sufficiently far from the others (the difference of opinions in distinct clusters exceeds the threshold):
 - only agents inside the same cluster interact
 - the dynamics leads to the convergence of the opinions of all agents in the cluster
- In general:
 - the *number and size of the clusters* depend on the threshold ϵ (if ϵ is small, more clusters emerge)
 - the parameter μ affects the convergence time
 - (when μ is small, the final cluster configuration also depends on μ)

Behavior of the Deffuant model



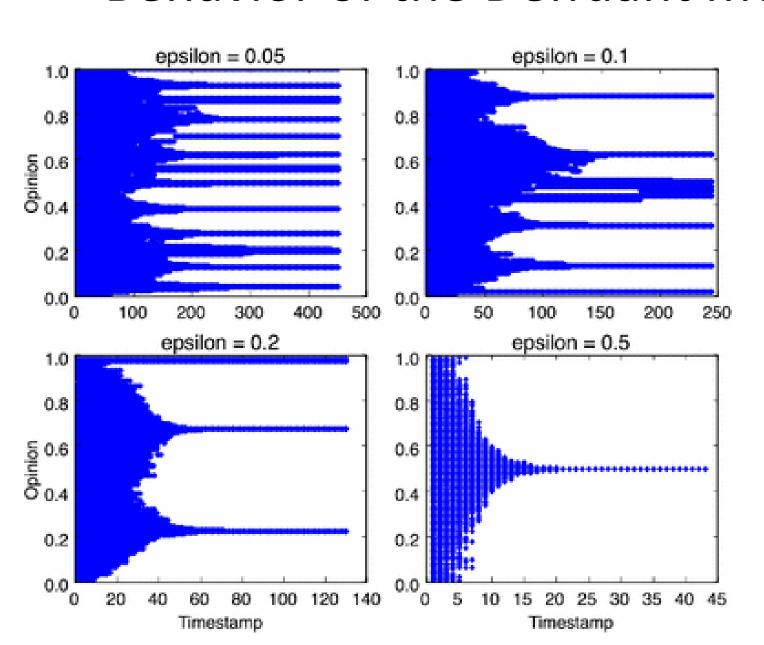
Opinion profile of a population of N=500 agents during its time evolution,

 $\varepsilon = 0.25$.

The population is fully mixed, i.e., everyone may interact with everybody else.

The dynamics leads to a polarization of the population in two factions.

Behavior of the Deffuant model



Hegselmann-Krause (HK) model

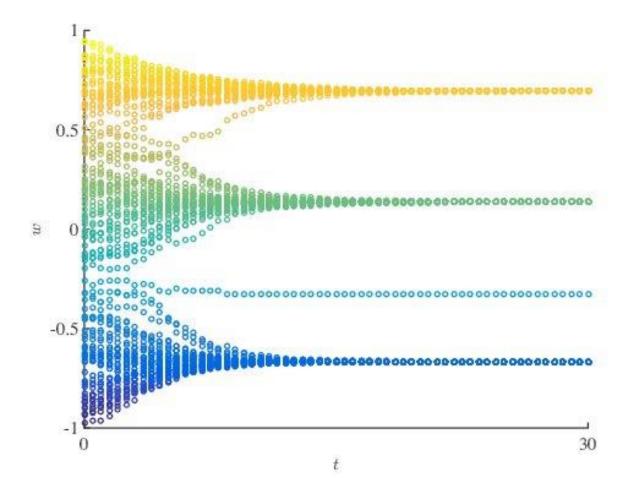
- Hegselmann and Krause, 2002
- Similarities with the Deffuant model:
 - Opinions take real values in an interval, say [0, 1]
 - An agent *i* (with opinion x_i), interacts with neighboring agents whose opinions lie in the range [x_i – ϵ , x_i + ϵ]
- Difference: update rule
 - An agent i does not interact with one of its compatible neighbors (like in Deffuant), but with all its compatible neighbors at once.
 - intended to describe formal meetings

$$x_i(t+1) = \frac{\sum_{j:|x_i(t) - x_j(t)| < \epsilon} a_{ij} x_j(t)}{\sum_{j:|x_i(t) - x_j(t)| < \epsilon} a_{ij}}$$

- a_{ii} : elements of an adjacency matrix describing the communication network.
- Agent i takes the average opinion of its compatible neighbors.

Behavior of the Hegselmann-Krause model

- fully determined by the uncertainty ε
- Need lot of computation power (due to the average calculation)



The dynamics develops similarly to the Deffuant model:

- Leads to the same pattern of stationary states, with the number of final opinion clusters decreasing if ε increases.
- for $\varepsilon > \varepsilon_c$ (a threshold) there can be only one cluster

Cultural dynamics

- Closely related to opinion dynamics (no clear border)
- Mostly: opinion: scalar variable

culture: a vector of variables (whose dynamics is inextricably coupled)

- The typical questions are similar:
 - what are the microscopic mechanisms that drive the formation of cultural domains?
 - What is the ultimate fate of diversity?
 - Is it bound to persist or all differences eventually disappear in the long run?
 - What is the role of the social network structure?

Axelrod model

- Axelrod, 1997
 - Attracted lot of interest both from social scientists and physicists
 - Reason (soc. sci): inclusion of two fundamental mechanisms:
 - Social influence: the tendency of individuals to become more similar when they interact
 - Homophily: the tendency of likes to attract each other, so that they interact more frequently
 - These two ingredients were generally expected (by social scientists) to generate a self-reinforcing dynamics leading to a global convergence to a single culture.
 - But it turns out that the model predicts in some cases the persistence of diversity.
 - From the viewpoint of stat. phys:
 - is a "vectorial" generalization of opinion dynamics models
 - gives rise to a very rich and nontrivial phenomenology, with some genuinely novel behavior

32

Axelrod's model

Individuals :

- are nodes on a network (or on the sites of a regular lattice original version)
- They are endowed with F integer variables $(\sigma_1, \ldots, \sigma_F)$ (describing their "culture")

The variables are the "cultural features"

- Each σ_i (feature) can assume q values: $\sigma_f = 0,1,...,q-1$
 - q: number of possible traits (modeling the different "beliefs, attitudes and behavior" of individuals

An elementary step:

- an individual i and one of his neighbors j are selected
- The overlap between them is computed:

$$\omega_{i,j} = \frac{1}{F} \sum_{f=1}^{F} \delta_{\sigma_f(i),\sigma_f(j)}$$

Where $\delta_{i,i}$ is the Kronecker delta

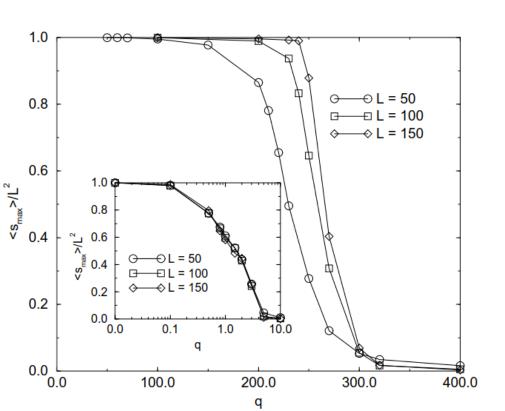
- $-\omega_{i,j}$: probability of interaction between i and j
 - If they interact: one of the features for which traits are different $(\sigma_f(i) \neq \sigma_f(j))$ is selected and the trait of the neighbor is set equal to $\sigma_f(i)$
 - If they do not interact: nothing happens

Features of the Axelrod model

- the dynamics tends to make interacting individuals more similar
- Interaction:
 - more likely for neighbors already sharing many traits (homophily)
 - Becomes impossible when no trait is the same
- For each a pair of neighbors: two stable configurations:
 - 1. when they are exactly equal, so that they belong to the same cultural region or
 - 2. when they are completely different, i.e., they sit at the border between cultural regions
- Starting from a disordered initial condition:
 - The evolution on any finite system leads to one of the many absorbing states, which belong to two classes:
 - 1. the ordered states, in which all individuals have the same set of variables, or
 - Frozen states with different coexisting cultural regions (more numerous)
- Which one is reached: depends on q (number of possible traits):
 - Small q: quickly full consensus is achieved
 - Large q: very few individuals share traits → few interactions occur →
 formation of small cultural domains that are not able to grow (disordered frozen state)

Order parameter and phase transition in the Axelrod model

- On regular lattices: the two regimes (full consensus vs. disordered frozen states) are separated by a *phase transition* at a critical value q_c , depending on F.
 - In one-dimensional systems the transition is continuous for all values of F
 - For two dimensions the nature of the transition depends on the value of F:
 - F = 2 there is a continuous change in the order parameter at q_c ,
 - for F > 2 the transition is discontinuous



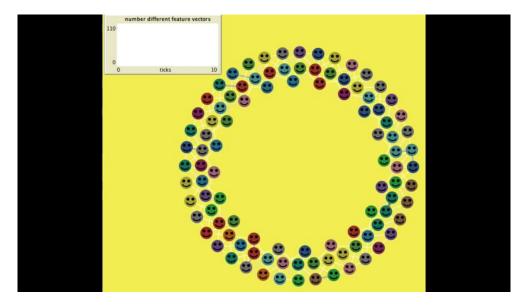
Order parameter: the average fraction $\langle S_{max} \rangle / N$ of the system occupied by the largest cultural region

- S_{max} :Fraction of the largest cultural region
- N: system size

Behavior of the order parameter vs. q for three different system sizes and F = 10. In the inset the same quantity is reported for F = 2.

35

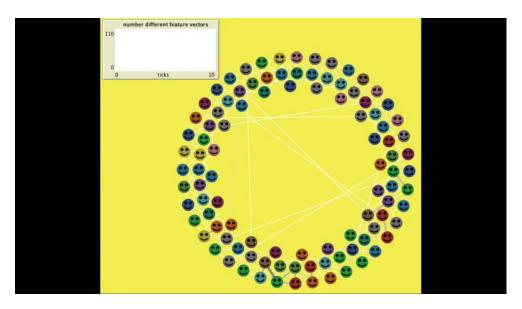
Axelrod's model of cultural dissemination in a circle network (16 sec)



- a circle interaction structure
- 100 agents, each
 - with 6 network contacts
 - 5 features
- Each feature can adopt 15 values
- Init: random set of traits
- Color of agents: one of the features
- Color and thickness of the lines: the overall similarity between the respective nodes
 - black thick lines: identical traits on all features
 - White thin lines: the two nodes are connected but maximally different.
- emergence of internally homogenous but mutually different clusters.
- Dynamics settled after 34,809 iterations with 19 cultural clusters.

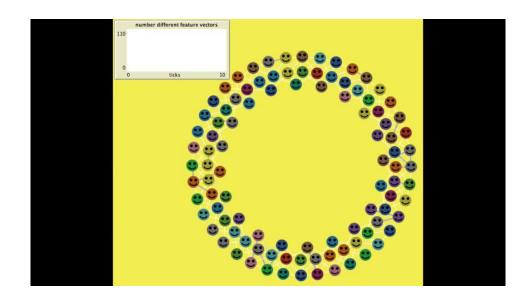
(Michael Maes, 2015)

Axelrod's model of cultural dissemination in a small world network (47 sec)



- a small-world interaction structure
- 100 agents, each
 - with 6 network contacts
 - 5 features
- Each feature can adopt 15 values
- Init: random set of traits
- Color of agents: one of the features
- Color and thickness of the lines: the overall similarity between the respective nodes
- emergence of internally homogenous but mutually maximally different clusters.
- Dynamics settled after 140,427 iterations with 7 cultural clusters.

Playing with Axelrod's model: the effect of globalization (53 sec)



- Globalization: more individuals are in contact with others who are geographically very distant
- Illustrates two implications of the model:
 - 1. due to the rewiring the number of clusters in equilibrium decreased from 22 to 16
 - 2. after the simulation continued (after rewiring) the number of unique combinations of cultural traits (diversity) first increased and then decreased
 - (i) globalization decreases cultural diversity
 - (ii) the short-term effects differ from the longterm effects
- Circle NW interaction structure (at the beginning!)
- 100 agents, each
 - with 6 network contacts
 - 5 features
- Each feature can adopt 15 values
- Init: random set of traits
- Color of agents: *one* of the features
- Color and thickness of the lines: the overall similarity between the respective nodes
- The dynamics reaches a rest point (after 51,065 iterations)
- Rewire 20 links and cont. (modeling that individuals have more contact to distant others)

(Michael Maes, 2015)

Information vs. belief

Information:

- A statement on its own
- If more, they do not form a system
- Modeled with a scalar (top most a series of scalars / vector)

Belief:

- They form a coherent system
- Converse's def: "a
 configuration of ideas
 and attitudes in which
 the elements are bound
 together by some form
 of constraint or
 functional
 interdependence

Two crucial aspects of belief dynamics

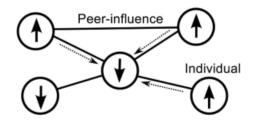
Cognitive bias (or belief bias):

- <u>Def</u>: A person's tendency to accept arguments that supports a conclusion that aligns with his/her values, beliefs and prior knowledge, while rejecting counter arguments to the conclusion
- Leads to individual belief rigidity

Social influence:

- The tendency of individuals to become more similar when they interact (we have seen it at the Axelrod model)
- Leads to social conformity

Social Factors

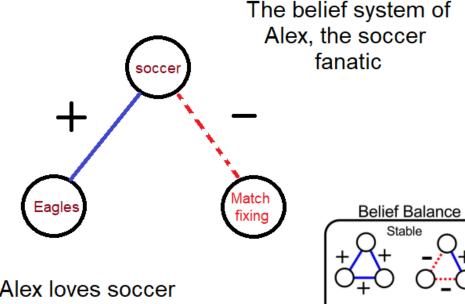


A cognitive-social model

- Individuals are embedded into a social NW, and social influence takes place via the social ties
- Each individual possesses a *network* of concepts and beliefs

The internal (in)coherence of each individual's belief network

is evaluated



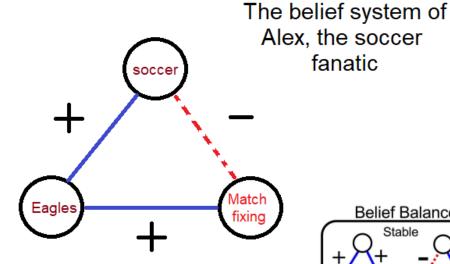
- 1) Alex loves soccer
- 2) Alex supports the Eagles

A cognitive-social model

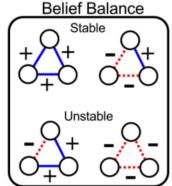
- Individuals are embedded into a social NW, and social influence takes place via the social ties
- Each individual possesses a network of concepts and beliefs

The internal (in)coherence of each individual's belief network

is evaluated



- 1) Alex loves soccer
- 2) Alex supports the Eagles
- The eagles has been with match fixing



A cognitive-social model

 The internal coherence of each individual's belief network is evaluated by the internal energy function (on the belief NW M):

(For simplicity, the belief NW is complete, meaning that all concepts have a positive or negative association with every other)

$$E_n^{(i)} = -\frac{1}{\binom{M}{3}} \sum_{j,k,l} a_{jk} a_{kl} a_{jl}$$

 The evolution of belief systems is also driven by social interactions: social energy term, capturing the degree of alignment between connected individuals.)

 k_{max} is a normalization factor, maximum degree of N.

$$E_n^{(s)} = -rac{1}{k_{max}igg(rac{M}{2}igg)} \sum_{q \in \Gamma(n)} ec{S}_n \cdot ec{S}_q$$

S: belief state vector: each element corresponds to an edge

Total energy:

where

I: peer-influence ,

J: coherentism

$$H = \sum_{n \in \mathcal{N}} \left[JE_n^{(i)} + IE_n^{(s)} \right]$$

- The status of the entire society is characterized by
 - (i) the average internal coherence of the individuals $\langle E^{(i)} \rangle$, and
 - (ii) the homogeneity of the society $\langle E^{(j)} \rangle$

The simulation:

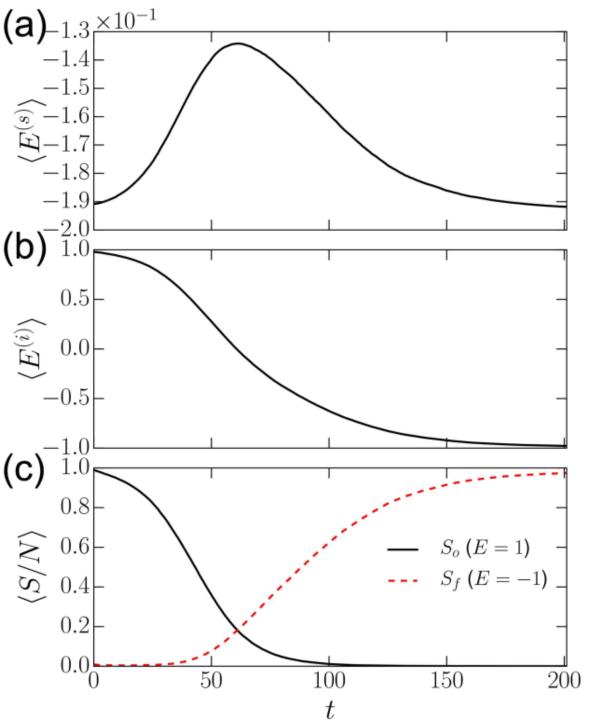
- At each time step a random pair of individuals is chosen
- One of the individuals (sender)randomly chooses a belief (association) from its internal belief system and sends it to the other individual (receiver)
- Assumption: each individual has an identical set of concept nodes
- The receiver accepts it if it decreases its individual energy H_n
- If $\Delta H_n > 0$, the receiver accepts it with probability $e^{-\Delta H_n}$
- T is "susceptibility" / "open-mindedness"

Results

- Given a homogeneous population of people with highly coherent belief systems, society remains stable.
- Given a homogeneous population of incoherent belief systems, society will become unstable and following a small perturbation, breaks down

In simulation:

- The society is initialized at consensus with an incoherent belief system.
- Then 1% of the population are given a random belief system
- Individuals attempt to reduce the energy of their own belief systems and leave consensus



In the simulation, the society is initialized at consensus with an incoherent belief system. Then 1% of the population are given a random belief system.

Strong societal consensus does not guarantee a stable society in our model. If major paradigm shifts occur and make individual belief systems incoherent, then society may become unstable.

- (a) The plot shows the evolution of social energy $E^{(s)}$ over time. The system starts at consensus but with incoherent beliefs. After introducing a small perturbation, individuals leave consensus, searching for more coherent sets of beliefs, until society reconverges at a stable configuration.
- **(b)** Decreasing mean individual energies $\langle E_{(i)} \rangle$ over time illustrates individual stabilization during societal transition.
- (c) $\langle S/N \rangle$ is the fractional group size. As society is upset, the original dominant but incoherent belief system S_o (solid black) is replaced by an emerging coherent alternative S_f (dashed red).

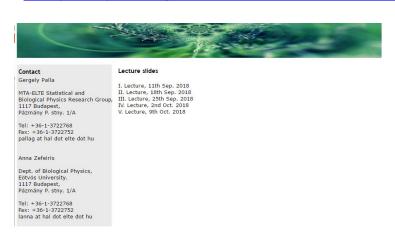
Information:

More literature on today's topic:

Castellano et al.: Statistical physics of social dynamics (2007), Sirbu et al: Opinion dynamics: models, extensions and external effects

Slides are available:

http://pallag.web.elte.hu/biostat/



http://hal.elte.hu/lanna/

